

# APPLIED ION SYSTEMS

## High Vacuum Engineering Calculations

Micro Propulsion Testing Chamber

Ultimate Pressure and System Gas Load Due to Outgassing for Pumpdown

### 1.) Maximum Theoretical Gas Loads for Ultimate Operating Pressures at Various Flows

#### a.) Ultimate Pressure vs. Working Pressure – Ideal Minimum Ratio

$$P_u = \frac{P_w}{10}$$

$P_u$ (Ultimate Pressure, Torr)	$P_w$ (Working Pressure, Torr)
$1 \times 10^{-8}$	$1 \times 10^{-7}$
$1 \times 10^{-7}$	$1 \times 10^{-6}$
$1 \times 10^{-6}$	$1 \times 10^{-5}$
$1 \times 10^{-5}$	$1 \times 10^{-4}$
$1 \times 10^{-4}$	$1 \times 10^{-3}$
$1 \times 10^{-3}$	$1 \times 10^{-2}$

#### b.) Pressure vs. Maximum Allowable Gas Load – Molecular Flow

$$S_e = \frac{q}{P_u} \rightarrow q = S_e \times P_u$$

$$S_e = 241.062 \text{ L/s for Water Vapor @ } 20\text{C}$$

$P$ (Pressure, Torr)	$q$ (Max Allowable Gas Load, Torr · L/s)
$1 \times 10^{-8}$	$2.411 \times 10^{-6}$
$1 \times 10^{-7}$	$2.411 \times 10^{-5}$
$1 \times 10^{-6}$	$2.411 \times 10^{-4}$
$1 \times 10^{-5}$	$2.411 \times 10^{-3}$
$1 \times 10^{-4}$	$2.411 \times 10^{-2}$

#### c.) Pressure vs. Maximum Allowable Gas Load –Transitional Flow

$$S_e = \frac{q}{P_u} \rightarrow q = S_e \times P_u$$

$$S_e = 93.771 \text{ L/s for Water Vapor @ } 20\text{C}$$

$P$ (Pressure, Torr)	$q$ (Max Allowable Gas Load, Torr · L/s)
$1 \times 10^{-3}$	$9.377 \times 10^{-2}$
$1 \times 10^{-2}$	$9.377 \times 10^{-1}$

## 2.) Total Gas Load

$$Q_{total} = Q_{volume} + Q_{leak} + Q_{outgas} + Q_{diffusion} + Q_{permeation} + Q_{backstreaming} + Q_{process}$$

→ assuming pumpdown ( $Q_{volume} = 0$  for bulk material),  $Q_{leak} = 0$ ,  $Q_{diffusion} = 0$ ,  $Q_{backstreaming} = 0$ ,  $Q_{process} = 0$ , and long term steady state pumping,

$$Q_{total} = Q_{outgas} + Q_{permeation}$$

$Q_{outgas} = \text{Total Sum of Outgassing Load} \times \text{Area per n Materials in System}$

$$Q_{outgas} = \sum_{1}^n q_{outgas} \times A$$

### a.) Gas Load of Diffusion Pump O-Ring

$$A_{o\_ring} = 87.553 \text{ cm}^2 \text{ (viton)}$$

$$L_{o\_ring} = 43.888 \text{ cm (viton)}$$

#### i. Unbaked, Pumped 1hr

$$QR_{outgas\_rate\_viton} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_o\_ring} = 7.004 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 2.787 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{diff\_o\_ring\_total} = 7.283 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

#### ii. Unbaked, Pumped >24hr

$$QR_{outgas\_rate\_viton} = 2.000 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_o\_ring} = 1.751 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 2.787 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{diff\_o\_ring\_total} = 4.538 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

#### iii. Baked, Pumped >24hr

$$QR_{outgas\_rate\_viton} = 5.000 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_o\_ring} = 4.380 \times 10^{-8} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 2.787 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{diff\_o\_ring\_total} = 2.831 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

### b.) Gas Load of Water Cooled Baffle Adapter:

$$A_{baffle\_adapter} = 195.996 \text{ cm}^2 \text{ (aluminum)}$$

$$A_{o\_ring} = 71.895 \text{ cm}^2 \text{ (viton)}$$

$$L_{o\_ring} = 64.819 \text{ cm (viton)}$$

#### i. Unbaked, Pumped 1hr

$$QR_{outgas\_rate\_aluminum} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_baffle\_adapter} = 1.568 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

$$QR_{outgas\_rate\_viton} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_viton} = 5.752 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 4.116 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{baffle\_adapter\_total} = 2.144 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

**ii. Unbaked, Pumped >24hr**

$$QR_{outgas\_rate\_aluminum} = 1.000 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_baffle\_adapter} = 1.960 \times 10^{-8} \text{ Torr} \cdot \text{L/s}$$

$$QR_{outgas\_rate\_viton} = 2.000 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_viton} = 1.438 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 4.116 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{baffle\_adapter\_total} = 5.574 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

**iii. Baked, Pumped >24hr**

$$QR_{outgas\_rate\_aluminum} = 5.000 \times 10^{-13} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_baffle\_adapter} = 9.800 \times 10^{-11} \text{ Torr} \cdot \text{L/s}$$

$$QR_{outgas\_rate\_viton} = 5.000 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_viton} = 3.590 \times 10^{-8} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 4.116 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{baffle\_adapter\_total} = 4.152 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

**c.) Gas Load of Water Cooled Baffle**

$$A_{baffle} = 2374.241 \text{ cm}^2 \text{ (stainless steel)}$$

$$A_{o\_ring} = 72.528 \text{ cm}^2 \text{ (viton)}$$

$$L_{o\_ring} = 65.389 \text{ cm (viton)}$$

**i. Unbaked, Pumped 1hr**

$$QR_{outgas\_rate\_stainless\_steel} = 5.000 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_baffle} = 1.190 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

$$QR_{outgas\_rate\_viton} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_viton} = 5.800 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

$$QR_{permeation\_rate\_viton} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{permeation\_o\_ring} = 4.150 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{baffle\_total} = 1.810 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

**ii. Unbaked, Pumped >24hr**

$$QR_{outgas\_rate\_stainless\_steel} = 1.000 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_baffle} = 2.370 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

$$QR_{outgas\_rate\_viton} = 2.000 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{outgas\_viton} = 1.450 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{permeation\_rate\_viton}} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{\text{permeation\_o\_ring}} = 4.150 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{\text{baffle\_total}} = 5.840 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

### iii. Baked, Pumped >24hr

$$QR_{\text{outgas\_rate\_stainless\_steel}} = 3.000 \times 10^{-13} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_baffle}} = 7.120 \times 10^{-10} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{outgas\_rate\_viton}} = 3.630 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_viton}} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{permeation\_rate\_viton}} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{\text{permeation\_o\_ring}} = 4.150 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{\text{baffle\_total}} = 4.190 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

## d.) Gas Load of Plate Adapter

$$A_{\text{plate\_adapter}} = 366.655 \text{ cm}^2 \text{ (aluminum)}$$

$$A_{\text{o\_ring}} = 34.872 \text{ cm}^2 \text{ (viton)}$$

$$L_{\text{o\_ring}} = 36.820 \text{ cm (viton)}$$

### i. Unbaked, Pumped 1hr

$$QR_{\text{outgas\_rate\_aluminum}} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_plate\_adapter}} = 2.933 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{outgas\_rate\_viton}} = 8.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_viton}} = 2.790 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{permeation\_rate\_viton}} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{\text{permeation\_o\_ring}} = 2.338 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{\text{plate\_adapter\_total}} = 3.236 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

### ii. Unbaked, Pumped >24hr

$$QR_{\text{outgas\_rate\_aluminum}} = 1.000 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_plate\_adapter}} = 3.667 \times 10^{-8} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{outgas\_rate\_viton}} = 2.000 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_viton}} = 6.974 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{permeation\_rate\_viton}} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{\text{permeation\_o\_ring}} = 2.338 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{\text{plate\_adapter\_total}} = 3.072 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

### iii. Baked, Pumped >24hr

$$QR_{\text{outgas\_rate\_aluminum}} = 5.000 \times 10^{-13} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_plate\_adapter}} = 1.833 \times 10^{-10} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{outgas\_rate\_viton}} = 5.000 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{\text{outgas\_viton}} = 1.744 \times 10^{-8} \text{ Torr} \cdot \text{L/s}$$

$$QR_{\text{permeation\_rate\_viton}} = 6.350 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}$$

$$Q_{\text{permeation\_o\_ring}} = 2.338 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{\text{plate\_adapter\_total}} = 2.356 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

e.) **Gas Load of Chamber:**

$$A_{chamber} = 2306.835 \text{ cm}^2 \text{ (stainless steel)}$$

$$A_{viewport} = 62.534 \text{ cm}^2 \text{ (glass)}$$

i. **Unbaked, Pumped 1hr**

$$Q_{R_{outgas\_rate\_stainless\_steel}} = 5 \times 10^{-8} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{chamber} = 1.153 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

$$Q_{R_{glass}} = 1.000 \times 10^{-7} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{viewport} = 6.253 \times 10^{-6} \text{ Torr} \cdot \text{L/s}$$

$$Q_{chamber\_total} = 1.216 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

ii. **Unbaked, Pumped >24hr**

$$Q_{R_{outgas\_rate\_stainless\_steel}} = 1 \times 10^{-10} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{chamber} = 2.307 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

$$Q_{R_{glass}} = 5.000 \times 10^{-9} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{viewport} = 3.127 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

$$Q_{chamber\_total} = 5.434 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

iii. **Baked, Pumped >24hr**

$$Q_{R_{outgas\_rate\_stainless\_steel}} = 3 \times 10^{-13} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{chamber} = 6.921 \times 10^{-10} \text{ Torr} \cdot \text{L/s}$$

$$Q_{R_{glass}} = 2.000 \times 10^{-9} \text{ Torr} \cdot \text{L/s} \cdot \text{cm}^2$$

$$Q_{viewport} = 1.251 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

$$Q_{chamber\_total} = 1.258 \times 10^{-7} \text{ Torr} \cdot \text{L/s}$$

f.) **TOTAL GAS LOAD:**

i. **Unbaked, Pumped 1hr**

$$Q_{total} = Q_{diff\_o\_ring\_total} + Q_{baffle\_adapter\_total} + Q_{baffle\_total} + Q_{plate\_adapter\_total} + Q_{chamber\_total}$$

$$Q_{total} = 7.283 \times 10^{-5} + 2.144 \times 10^{-4} + 1.810 \times 10^{-4} + 3.236 \times 10^{-4} + 1.216 \times 10^{-4}$$

$$Q_{total} = 9.134 \times 10^{-4} \text{ Torr} \cdot \text{L/s}$$

ii. **Unbaked, Pumped >24hr**

$$Q_{total} = Q_{diff\_o\_ring\_total} + Q_{baffle\_adapter\_total} + Q_{baffle\_total} + Q_{plate\_adapter\_total} + Q_{chamber\_total}$$

$$Q_{total} = 4.538 \times 10^{-6} + 5.574 \times 10^{-6} + 5.840 \times 10^{-6} + 3.072 \times 10^{-6} + 5.434 \times 10^{-7}$$

$$Q_{total} = 1.957 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

iii. **Baked, Pumped >24hr**

$$Q_{total} = Q_{diff\_o\_ring\_total} + Q_{baffle\_adapter\_total} + Q_{baffle\_total} + Q_{plate\_adapter\_total} + Q_{chamber\_total}$$

$$Q_{total} = 2.831 \times 10^{-6} + 4.152 \times 10^{-6} + 4.190 \times 10^{-6} + 2.356 \times 10^{-6} + 1.258 \times 10^{-7}$$

$$Q_{total} = 1.365 \times 10^{-5} \text{ Torr} \cdot \text{L/s}$$

### 3.) Maximum Achievable Vacuum During Pumpdown

a.) Unbaked, Pumped 1hr

$$S_e = \frac{q}{P_u}$$

$$P_u = \frac{q}{S_e}$$

$S_e = 241.062 \text{ L/s for Water Vapor @ 20C in Molecular Flow}$

$q = 7.970 \times 10^{-4} \text{ Torr} \cdot \text{L/s Unbaked, Pumped} < 1\text{hr}$

$$P_u = 3.789 \times 10^{-6} \text{ Torr}$$

b.) Unbaked, Pumped >24hr

$$S_e = \frac{q}{P_u}$$

$$P_u = \frac{q}{S_e}$$

$S_e = 241.062 \text{ L/s for Water Vapor @ 20C in Molecular Flow}$

$q = 1.903 \times 10^{-5} \text{ Torr} \cdot \text{L/s Unbaked, Pumped} > 24\text{hr}$

$$P_u = 8.117 \times 10^{-8} \text{ Torr}$$

c.) Baked, Pumped >24hr

$$S_e = \frac{q}{P_u}$$

$$P_u = \frac{q}{S_e}$$

$S_e = 241.062 \text{ L/s for Water Vapor @ 20C in Molecular Flow}$

$q = 1.353 \times 10^{-5} \text{ Torr} \cdot \text{L/s Baked, Pumped} > 24\text{hr}$

$$P_u = 5.664 \times 10^{-8} \text{ Torr}$$

### 4.) Critical Factor Determination for Feasibility of Pumping System

→ Critical Pumping Speed  $\geq 0.01 \text{ L/s/cm}^2$

→ Critical Pumping Speed =  $241.062 \text{ L/s} / 2369.369 \text{ cm}^2$

→ Critical Pumping Speed =  $0.102 \text{ L/s/cm}^2$  (total chamber area)

→ Critical Pumping Speed IS VALID