

High Vacuum System Engineering Calculations
2.75" Conflat High Vacuum System
Design Iteration #4
Molecular Flow with Water Vapor at 20C

**CONDUCTANCE CALCULATIONS – MOLECULAR FLOW
(For Use with General Pump-Down @ < 10⁻³ Torr)**

1.) Diffusion Pump

→ Max Pumping Speed of Diffusion Pump (Air)

→ **$S_{diff} = 600 \text{ l/sec}$**

2.) Diffusion Pump to Water Cooled Baffle Adapter (@ 20C)

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 18.020 (average AMU of air)

D = diameter (cm) = 10.668

L = length (cm) = 1.27

$C_m = 14651.985 \text{ l/sec}$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 14651.985

D = diameter (cm) = 10.668

L = length (cm) = 1.27

$C_{short} = 1200.982 \text{ l/sec}$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.119$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$C_{shortFinal} = 1056.864 \text{ l/sec}$

→ Correction for Extended Baffle Fins

$$C_{shortFinal} = C_{short} \times 0.50$$

$C_{shortFinal} = 528.432 \text{ l/sec}$

→ **$C_{baffle_adapter} = 528.432 \text{ l/sec}$**

3.) Water Cooled Baffle (@ 20C)

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 18.020 (average AMU of air)

D = diameter (cm) = 10.605

L = length (cm) = 2.032

$$C_m = \mathbf{8996.208 \text{ l/sec}}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 8996.208

D = diameter (cm) = 10.605

L = length (cm) = 2.032

$$C_{short} = \mathbf{1130.367 \text{ l/sec}}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.192$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$$C_{shortFinal} = \mathbf{994.723 \text{ l/sec}}$$

→ Correction for Baffle Fins

$$C_{shortFinal} = C_{short} \times 0.50$$

$$C_{shortFinal} = \mathbf{392.255 \text{ l/sec}}$$

→ **$C_{baffle} = 497.128 \text{ l/sec}$**

4.) Diffusion Pump to 2.75" Conflat Adapter Plate

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 18.020 (average AMU of water vapor)

D = diameter (cm) = 3.556

L = length (cm) = 2.54

$$C_m = \mathbf{271.333 \text{ l/sec}}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 271.333

D = diameter (cm) = 3.556

L = length (cm) = 2.54

$$C_{short} = \mathbf{94.561 \text{ l/sec}}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.714$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$$C_{shortFinal} = \mathbf{83.293 \text{ l/sec}}$$

→ **$C_{plate \text{ adapter}} = 83.293 \text{ l/sec}$**

5.) 2.75" Conflat 4-Way Cross

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 18.020 (average AMU of water vapor)

D = diameter (cm) = 3.556

L = length (cm) = 12.492

$$C_m = \mathbf{55.170 \text{ l/sec}}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 43.511

D = diameter (cm) = 3.556

L = length (cm) = 12.492

$$C_{short} = \mathbf{39.991 \text{ l/sec}}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 3.5$$

~+9% error max:

$$C_{shortFinal} = C_{short} \times 0.91$$

$$C_{shortFinal} = \mathbf{36.392 \text{ l/sec}}$$

→ **$C_{cross} = 36.392 \text{ l/sec}$**

6.) 2.75" Conflat Gate Valve

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 18.020 (average AMU of water vapor)

D = diameter (cm) = 3.810

L = length (cm) = 5.050

$$C_m = \mathbf{166.864 \text{ l/sec}}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L}\right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 166.864

D = diameter (cm) = 3.556

L = length (cm) = 2.54

$$C_{short} = 83.432 \text{ l/sec}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.714$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$$C_{shortFinal} = 73.420 \text{ l/sec}$$

→ $C_{gate_valve} = 73.420 \text{ l/sec}$

7.) TOTAL SYSTEM CONDUCTANCE

→ Conductance of Pipeline

$$\frac{1}{C_{pipeline}} = \frac{1}{C_{baffle_adapter}} + \frac{1}{C_{baffle}} + \frac{1}{C_{plate_adapter}} + \frac{1}{C_{cross}} + \frac{1}{C_{gate_valve}}$$
$$\frac{1}{C_{pipeline}} = \frac{1}{528.432} + \frac{1}{497.128} + \frac{1}{83.293} + \frac{1}{36.392} + \frac{1}{73.420}$$
$$C_{pipeline} = 17.541 \text{ l/sec}$$

→ $C_{pipeline} = 17.541 \text{ l/sec}$

→ Effective Pumping Speed of the System

$$\frac{1}{S_e} = \frac{1}{C_{pipeline}} + \frac{1}{S_{diff}}$$

$$S_e = \frac{C_{pipeline} \times S_{diff}}{C_{pipeline} + S_{diff}}$$

$$C_{pipeline} = 17.541 \text{ l/s}$$

$$S_{diff} = 600 \text{ l/s}$$

$$S_e = 17.043 \text{ l/s}$$

→ $S_e = 17.043 \text{ l/sec}$