

High Vacuum System Engineering Calculations
2.75" Conflat High Vacuum System
Design Iteration #4
Molecular Flow with Deuterium at 20C

CONDUCTANCE CALCULATIONS – MOLECULAR FLOW
(For Use with Injected Deuterium Beam Neutron Systems @ < 10⁻³ Torr)

1.) Diffusion Pump

→ Max Pumping Speed of Diffusion Pump (Hydrogen)

→ **$S_{diff} = 800 \text{ l/sec}$**

2.) Diffusion Pump to Water Cooled Baffle Adapter (@ 20C)

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 2.014 (average AMU of deuterium)

D = diameter (cm) = 10.668

L = length (cm) = 1.27

$C_m = 43827.239 \text{ l/sec}$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 43827.239

D = diameter (cm) = 10.668

L = length (cm) = 1.27

$C_{short} = 3592.397 \text{ l/sec}$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.119$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$C_{shortFinal} = 3161.309 \text{ l/sec}$

→ Correction for Extended Baffle Fins

$$C_{shortFinal} = C_{short} \times 0.50$$

$C_{shortFinal} = 1580.655 \text{ l/sec}$

→ **$C_{baffle_adapter} = 1580.655 \text{ l/sec}$**

3.) Water Cooled Baffle (@ 20C)

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 2.014 (average AMU of deuterium)

D = diameter (cm) = 10.605

L = length (cm) = 2.032

$$C_m = \mathbf{26909.593 \text{ l/sec}}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 26909.593

D = diameter (cm) = 10.605

L = length (cm) = 2.032

$$C_{short} = \mathbf{3381.171 \text{ l/sec}}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.192$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$$C_{shortFinal} = \mathbf{2975.430 \text{ l/sec}}$$

→ Correction for Baffle Fins

$$C_{shortFinal} = C_{short} \times 0.50$$

$$C_{shortFinal} = \mathbf{1487.715 \text{ l/sec}}$$

→ **$C_{baffle} = 1487.715 \text{ l/sec}$**

4.) Diffusion Pump to 2.75" Conflat Adapter Plate

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 2.014 (average AMU of deuterium)

D = diameter (cm) = 3.556

L = length (cm) = 2.54

$$C_m = \mathbf{811.616 \text{ l/sec}}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 811.616

D = diameter (cm) = 3.556

L = length (cm) = 2.54

$$C_{short} = \mathbf{283.122 \text{ l/sec}}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.714$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$$C_{shortFinal} = 249.147 \text{ l/sec}$$

→ **$C_{plate\ adapter} = 249.147 \text{ l/sec}$**

5.) 2.75" Conflat 4-Way Cross

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 2.014 (average AMU of deuterium)

D = diameter (cm) = 3.556

L = length (cm) = 12.492

$$C_m = 165.026 \text{ l/sec}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L} \right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 37.054

D = diameter (cm) = 3.556

L = length (cm) = 12.492

$$C_{short} = 119.623 \text{ l/sec}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 3.5$$

~+9% error max:

$$C_{shortFinal} = C_{short} \times 0.91$$

$$C_{shortFinal} = 108.857 \text{ l/sec}$$

→ **$C_{cross} = 108.857 \text{ l/sec}$**

6.) 2.75" Conflat Gate Valve

→ Conductance of a Tube

$$C_m = 3.8 \left(\frac{T}{M} \right)^{\frac{1}{2}} \frac{D^3}{L}$$

C_m = conductance (l/sec)

T = temperature (K) = 293.15

M = molecular mass = 2.014 (average AMU of deuterium)

D = diameter (cm) = 3.810

L = length (cm) = 5.080

$$C_m = 499.126 \text{ l/sec}$$

→ Conductance of a Short Tube

$$C_{short} = C_m \left(1 + \frac{4D}{3L}\right)^{-1}$$

C_{short} = conductance of short tube (l/sec)

C_m = conductance of a long tube (l/sec) = 499.126

D = diameter (cm) = 3.810

L = length (cm) = 2.54

$$C_{short} = 249.563 \text{ l/sec}$$

→ for $L/D < 5$, above equation is valid for short pipes, with error

$$L/D = 0.714$$

~+12% error max:

$$C_{shortFinal} = C_{short} \times 0.88$$

$$C_{shortFinal} = 219.615 \text{ l/sec}$$

→ $C_{butterfly_valve} = 219.615 \text{ l/sec}$

7.) TOTAL SYSTEM CONDUCTANCE

→ Conductance of Pipeline

$$\frac{1}{C_{pipeline}} = \frac{1}{C_{baffle_adapter}} + \frac{1}{C_{baffle}} + \frac{1}{C_{plate_adapter}} + \frac{1}{C_{cross}} + \frac{1}{C_{gate_valve}}$$
$$\frac{1}{C_{pipeline}} = \frac{1}{1580.655} + \frac{1}{1487.715} + \frac{1}{249.147} + \frac{1}{108.857} + \frac{1}{219.615}$$
$$C_{pipeline} = 52.471 \text{ l/sec}$$

→ $C_{pipeline} = 52.471 \text{ l/sec}$

→ Effective Pumping Speed of the System

$$\frac{1}{S_e} = \frac{1}{C_{pipeline}} + \frac{1}{S_{diff}}$$

$$S_e = \frac{C_{pipeline} \times S_{diff}}{C_{pipeline} + S_{diff}}$$

$$C_{pipeline} = 52.471 \text{ l/s}$$

$$S_{diff} = 800 \text{ l/s}$$

$$S_e = 49.241 \text{ l/s}$$

→ $S_e = 49.241 \text{ l/sec}$